

University of International Business and Economics International Summer School

MAT 120 Calculus II

Term: July 13 - August 7, 2020

Instructor: Shen Fan

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Office Hours: TBD

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Class Hours: Monday through Friday, 120 minutes each day (2,400 minutes in total)

Discussion session: 2 hours each week

Total Contact Hours: 64 contact hours (45 minutes each, 48 hours in total)

Credit: 4 units

Course Description:

In this course, the student will gain knowledge of the basic theory of integrals and proficiency with various standard techniques of integration: integration by parts, trigonometric substitution, partial fraction decomposition, etc. The student will also be exposed to certain traditional applications of those techniques: calculation of volumes (of solids of revolution, for example) and arc lengths, and the solution of some elementary differential equations. The student will be introduced to the theory of sequences and series, and the approximation of functions using series.

Course Goals:

A student who satisfactorily completes this course will:

- Have facility with the basic theory and techniques of integral calculus (the Fundamental Theorem of Calculus, integration by parts, etc.) and have an understanding of why the theory and techniques are valid.
- Have precise knowledge of the definitions and theorems from the basic theory of sequences and series: convergence of sequences, partial sums, series convergence, absolute convergence, conditional convergence, Integral Test, Comparison Test, etc.
- Have facility with basic calculational skills: evaluation of integrals using the basic techniques
 of integral calculus, calculation of volumes and arc length, solution of elementary
 differential equations, determination of convergence or divergence of sequences and
 series, calculation of radius of convergence of power series, determination of the power
 series representation of appropriate functions, etc.
- Have a rudimentary ability to explain mathematical theory (e.g., why integration by parts works, etc.) using rigorous mathematical reasoning.



Required Text:

Stewart, James. Single Variable Essential Calculus: Early Transcendentals, 8th edition

Prerequisites:

The course is based on Calculus I or its equivalent. Students are expected to know basic concepts of calculus for functions of a single real variable. They include: basic elementary functions and their properties, differentiation and geometrical significance of the derivative, definite and indefinite integrals, Fundamental Theorem of Calculus, indefinite integrals of basic elementary functions.

Attendance policy:

Summer school is very intense and to be successful, students need to attend <u>every class</u>. Occasionally, due to illness or other unavoidable circumstance, a student may need to miss a class. A medical certificate is required to be excused. Any absence may impact on the student's grade. Arriving late or leaving early will count as a partial absence. If a student is missing less than a point for a better grade, the better grade will be given, provided the student had no unexcused absences during the course.

Academic honesty:

Students are expected to maintain high standards of academic honesty. Specifically, no notes, no electronic devices, no books are permitted on Exams. One formula sheet on a piece of paper of a standard format (e.g., A4) is allowed on Exams. Admission to Exams is only with a picture ID. Zero tolerance to any kind of cheating (e.g., copying solutions from classmates, use of unauthorized materials or devices). Failure to abide by this will result in a zero score on the examination, or even failure in the course.

Grading Policy:

There will be daily quizzes, three midterms and one final exam in this class. All exams will be closed-book. No notes, calculators, or other electronic devices will be allowed, and having such a device in view during the exam is an academic honesty violation.

| Α | 90 and above | C+ | 65-69 |
|----|--------------|----|----------|
| A- | 85-89 | С | 60-64 |
| B+ | 80-84 | C- | 55-59 |
| В | 75-79 | D | 50-54 |
| B- | 70-74 | F | below 50 |

It should be noted that in many US colleges **C**- is not a passing grade if the course is required for a major.



Grading Scale:

The course grades will be calculated based on the following percentages:

Quizzes: 10%
Midterm 1: 20%
Midterm 2: 20%
Midterm 2: 20%
Final Exam: 30%

The final exam will be cumulative. There will be no make-up exams.

Class Rules:

All academic work should be done with the high level of honesty and integrity. Academic misconduct of any kind may result in a grade penalty or the assignment of a failing grade.

Course Schedule:

The planned schedule sketched out below may be modified to suit the interests or abilities of the enrolled students or to take advantage of special opportunities or events that may arise during the term.

Week 1 7/13-7/17

Assignment

The Fundamental Theorem of Calculus; Integration by Substitution

5.4: 2, 6, 7, 10, 13, 16, 25

5.5: 3, 5, 8, 10, 11, 24, 37, 38, 40

Integration by Parts; Trigonometric Substitution

6.1: 5, 6, 14, 17, 25, 29, 34, 42

6.2: 3, 5, 14, 15, 19, 35, 37, 40, 42, 60

Partial Fraction Decomposition

6.3: 5, 10, 12, 23, 27, 29, 37, 41

Approximate Integration

6.5: 7, 9, 13, 17, 25, 26, 27, 34, 35

Improper Integrals

6.6: 2, 8, 11, 13, 20, 22, 31, 32, 41, 50, *60

Exam 1: Date TBD Week 2 7/20-7/24

Assignment

Areas between Curves; Volumes

7.1: 3, 6, 8, 13, 21, 27, 29, 32

7.2: 2, 5, 7, 13, 15, 21, 27, 29, 39

Volumes by Cylindrical Shells

7.3: 11, 13, 17, 20, 21, 29, 33, 41, 42

Arc Length

7.4: 3, 7, 9, 14, 17, 27, 30



Applications to Physics and Engineering

7.5: 5, 6, 9, 13, 15, 21, 27, 29, 32, 39, 41, 43

Exam 2;

Differential Equations

7.6: 2, 3, 9, 15, 23, 33, 36, *47

Week 3 7/27-7/31

Assignment

Sequences

8.1: 1, 9, 11, 15, 21, 23, 24, 25, 31, 33, 34, 41, 42, *46

Series

8.2: 7, 8, 10 11 12 19, 21 39, 42, 43, 47, 50

Exam 3: Date TBD

Integral Test; Comparison Test

8.3: 1, 3, 6, 11, 13, 15, 21, 25, 27, 28, 35, 39

Root Test; Ratio Test

8.4: 1, 2, 5, 11, 19, 21, 25, 27, 33, 37, 39, 41, *43

Exam 3;

Power Series

8.5: 2, 3, 7, 8, 13, 17, 18, 19, 20, 29

Week 4 8/3-8/7

Assignment

Functions as Power Series

8.6: 1, 13, 14, 15, 23, 27, 32, 35, 37

Taylor and Maclaurin Series

8.7: 2, 5, 13, 14, 25, 27, 43

Taylor and Maclaurin Series

8.7: 47, 53, 55, 59, 60, 65

Applications of Taylor and Maclaurin Series

8.8: 9, 10 13, 19, 20, 23, 25, 26, *30

Final Exam

General Comments:

- 1. In order to train your minds in mathematical thinking, much of lecture will consist of the "Socratic Method" of questioning. Even if silently, do try to puzzle out the answers. An analogy: the lecture should be a "mental exercise" class. Knowledge cannot be given: it must be stolen. Engage your mind.
- 2. Many problems will not be solvable at first (or second) viewing. Be patient: clarify any unknown concepts, try to reduce the problem, brainstorm to unearth possibly relevant concepts, and follow your intuition. It may help to, after a period of hard work, put the problem away. Do not worry if you cannot do every problem: what is important is that you try.
- 3. If you find yourself getting lost in the material, come to office hours immediately! It is much is easier to lead a student's mind individually rather than in a group.
- 4. Note that we may not dot every i or cross every t in class: you are responsible for reading the



text. In particular, it is to your advantage to read the material before coming to class; in this way the student becomes an active participant rather than a passive recipient.

- 5. Basic etiquette should be maintained. For example: to give your classmates time to think, please do not blurt out answers unless called upon (or overcome with excitement); please do not walk out of class without prior explanation, etc.
- 6. Using a cell phone in class is not permitted; students using phones will be penalized 5 percentage points on the next exam.
- 7. Tests will check your understanding of the lectures as well as cover homework-type problems; it will benefit you to check after each lecture to see if you've understood the line of the arguments.

Precise knowledge of the theory is vital!